

# Computer Science Pre-Ph.D. Qualifying Exam

## 1- Advanced Algorithms ->

الخوارزميات المتقدمة

**Reference:** Introduction to Algorithms (Any Edition), Cormen, Leiserson, Rivest, and Stein (CLRS)

### **Topics:**

1. Divide and conquer:
  - Asymptotic analysis including big-oh notation
  - Divide-and-conquer algorithms for sorting, counting inversions, matrix multiplication, closest pair, and selection.
  - Running time analysis of divide-and-conquer algorithms.
  - The master method.
2. Randomized algorithms:
  - Randomized QuickSort.
  - Randomized selection.
  - Computing the median in linear time.
  - A randomized algorithm for the minimum graph cut problem.
3. Graph algorithms:
  - Graph primitives.
  - Depth- and breadth-first search.
  - Connected components in undirected graphs.
  - Topological sort in directed acyclic graphs.
  - Strongly connected components in directed graphs.
  - Dijkstra's shortest-path algorithm.
4. Advanced data structures:
  - Heaps and applications.
  - Hash tables and applications.
  - Balanced binary search trees.
  - Union-Find Data Structure.
5. Greedy algorithms:
  - Scheduling.
  - Prim's Minimum Spanning Tree Algorithm.
  - Kruskal's Minimum Spanning Tree Algorithm.
  - Clustering.
  - Huffman Codes.
6. Dynamic Programming:
  - The Knapsack Problem.
  - Sequence Alignment.
  - Optimal Search Trees.
  - Single-Source Shortest Paths (The Bellman-Ford Algorithm)
  - Internet Routing.
  - The All-Pairs Shortest Paths Problem.
  - The Floyd-Warshall Algorithm.
  - Johnson's Algorithm.

## 7. NP-Completeness:

- P, NP, and What They Mean.
- Reductions between Problems.
- NP-Complete Problems.
- The P vs. NP Problem.
- Solvable Special Cases of NP-Complete Problems.
- Smarter (But Still Exponential-Time) Search Algorithms for NP-Complete Problems (Vertex Cover Problem)
- Heuristics with Provable Guarantees (Approximation Algorithms).
- Greedy and Dynamic Programming Heuristics for the Knapsack Problem.
- Local Search: General Principles, Max Cut, and 2SAT.

**Support Material:** The exam topics are covered in the following online courses:

<https://class.coursera.org/algo-004/lecture/preview>

<https://class.coursera.org/algo2-2012-001/lecture/preview>

The slides are also available at:

<http://theory.stanford.edu/~tim/mooc/algo1slides.zip>

<http://theory.stanford.edu/~tim/mooc/algo2slides.zip>

## 2- Theory of Computation ->

نظرية الحسابات

### References:

- James L. Hein, "Theory of Computation: An introduction", Jones and Bartlett Publishers, 1996.
- Daniel I. A. Cohen, "Introduction to Computer Theory", 2nd Edition, Wiley & Sons, 1997.

### • Regular Languages and Finite Automata

- Regular Expressions
- Deterministic Finite Automata (DFA)
- Nondeterministic Finite Automata (NFA)
- Transforming Regular Expressions into Finite Automata
- Transforming Finite Automata into Regular Expressions
- Transforming NFA into DFA
- Minimize States of DFAs
- Finite Automata as Output devices
- Representing and Executing Finite Automata
- Regular Grammars
- Properties of Regular Languages

- **Context-Free Languages and Pushdown Automata**
  - Context-Free Languages
  - Context-Free Grammars
  - Pushdown Automata
  - Representing and Executing Pushdown Automata
  - Parsing Techniques
- **Turing Machines and Equivalent Models**
  - Turing Machines with Output
  - Universal Turing Machines
  - Simple Programming Languages
- **Computational Complexity**
  - Optimal Algorithms
  - Comparing Rates of Growth
  - Complexity Classes